

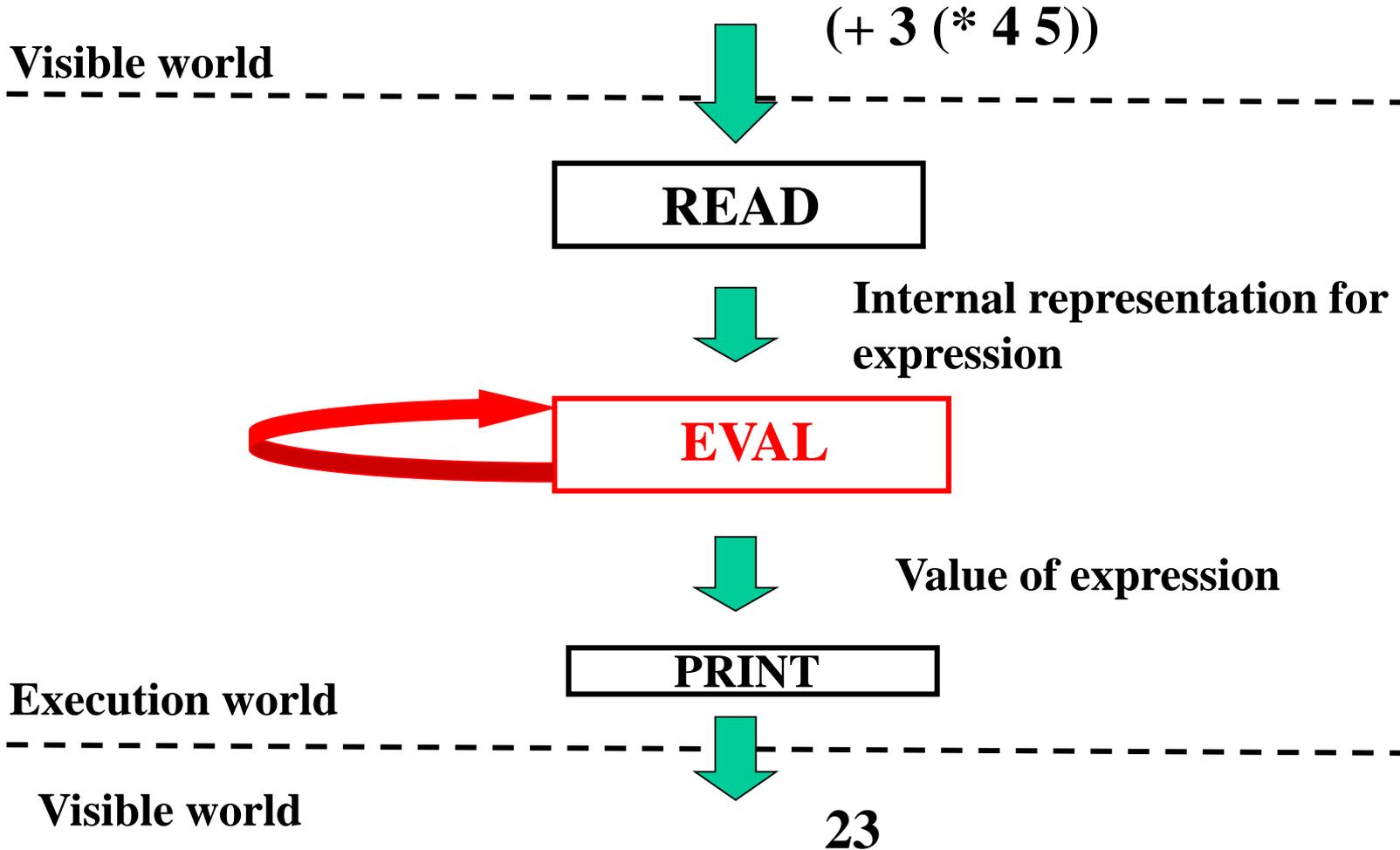
Basic Scheme February 8, 2007

- Compound expressions
- Rules of evaluation
- Creating procedures by capturing common patterns

Previous lecture

- Basics of Scheme
 - Expressions and associated values (or syntax and semantics)
 - Self-evaluating expressions
 - 1, “this is a string”, #f
 - Names
 - +, *, >=, <
 - Combinations
 - (* (+ 1 2) 3)
 - Define
- Rules for evaluation

Read-Eval-Print



Summary of expressions

- **Numbers:** value is expression itself
- **Primitive procedure names:** value is pointer to internal hardware to perform operation
- **“Define”:** has no actual value; is used to create a binding in a table of a name and a value
- **Names:** value is looked up in table, retrieving binding
- Rules apply recursively

Simple examples

25	→	25
(+ (* 3 5) 4)	→	60
+	→	[#primitive procedure ...]
(define foobar (* 3 5))	→	no value, creates binding of foobar and 15
foobar	→	15 (value is looked up)
(define fred +)	→	no value, creates binding
(fred 3 5)	→	15

This lecture

Adding procedures and procedural abstractions to capture processes

Language elements -- procedures

- Need to capture ways of doing things – use procedures

(lambda (x) (* x x))

parameters (points to **(x)**)
body (points to **(* x x)**)

To process something (points to **(lambda**)
multiply it by itself (points to **(* x x)**)



- Special form – creates a procedure and returns it as value

Language elements -- procedures

- Use this anywhere you would use a procedure

`((lambda(x)(* x x)) 5)`



`(* 5 5)` lambda exp

arg

Language elements -- abstraction

- Use this anywhere you would use a procedure
`((lambda(x)(* x x)) 5)`

Don't want to have to write obfuscatory code – so can give the lambda a name

`(define square (lambda (x) (* x x)))`
`(square 5) → 25`

Rumplestiltskin effect!
(The power of naming things)

Scheme Basics

- Rules for *evaluating*
 1. If **self-evaluating**, return value.
 2. If a **name**, return value associated with name in environment.
 3. If a **special form**, do something special.
 4. If a **combination**, then
 - a. *Evaluate* all of the subexpressions of combination (in any order)
 - b. *apply* the operator to the values of the operands (arguments) and return result
- Rules for *applying*
 1. If procedure is **primitive procedure**, just do it.
 2. If procedure is a **compound procedure**, then:
evaluate the body of the procedure with each formal parameter replaced by the corresponding actual argument value.

Interaction of define and lambda

1. `(lambda (x) (* x x))`
 `==> #[compound-procedure 9]`
2. `(define square (lambda (x) (* x x)))`
 `==> undef`
3. `(square 4)` `==> 16`
4. `((lambda (x) (* x x)) 4)` `==> 16`
5. `(define (square x) (* x x))` `==> undef`

This is a convenient shorthand (called “syntactic sugar”) for 2 above – this is a use of lambda!

Lambda special form

- lambda syntax `(lambda (x y) (/ (+ x y) 2))`
- 1st operand position: the **parameter list** `(x y)`
 - a list of names (perhaps empty) `()`
 - determines the number of operands required
- 2nd operand position: the **body** `(/ (+ x y) 2)`
 - may be any expression(s)
 - not evaluated when the lambda is evaluated
 - evaluated when the procedure is applied
 - value of body is value of last expression evaluated
- mini-quiz: `(define x (lambda () (+ 3 2)))`
 - `x`
 - `(x)`
- semantics of lambda:

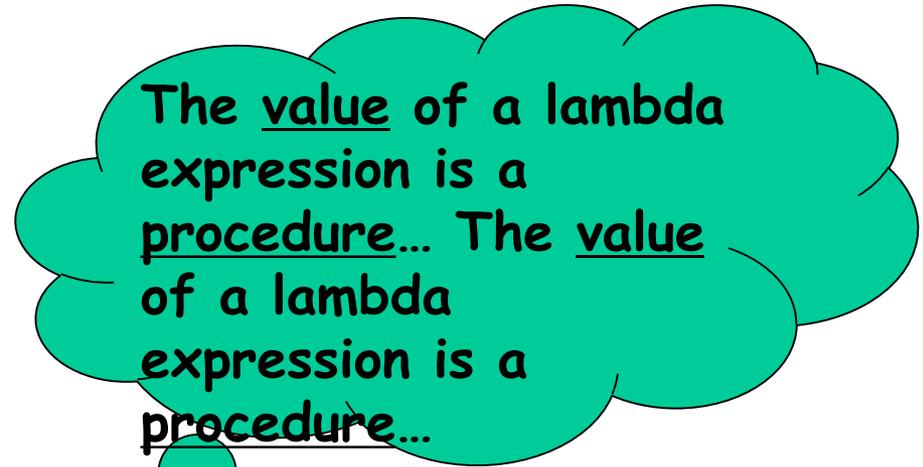
**THE VALUE OF
A LAMBDA EXPRESSION
IS
A PROCEDURE**

Achieving Inner Peace

(and a good grade)



**Om Mani Padme Hum...*



Using procedures to describe processes

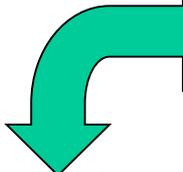
- How can we use the idea of a procedure to capture a computational process?

What does a procedure describe?

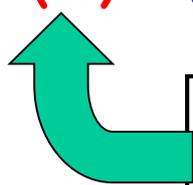
- Capturing a common pattern
 - (* 3 3)
 - (* 25 25)
 - (* foobar foobar)

(lambda (x) (* x x))

Common pattern to capture



Name for thing that changes



Modularity of common patterns

Here is a common pattern:

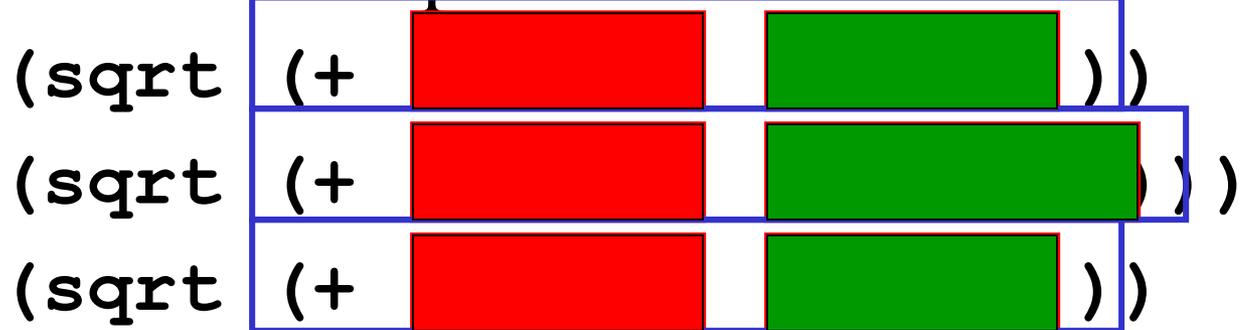
```
(sqrt (+ (* 3 3) (* 4 4)))  
(sqrt (+ (* 9 9) (* 16 16)))  
(sqrt (+ (* 4 4) (* 4 4)))
```

Here is one way to capture this pattern:

```
(define pythagoras  
  (lambda (x y)  
    (sqrt (+ (* x x) (* y y))))))
```

Modularity of common patterns

Here is a common pattern:



The diagram shows three lines of code, each enclosed in a blue box. The code is: `(sqrt (+ [red box] [green box]))`. The red box highlights the expression inside the `+` operator, and the green box highlights the expression inside the `sqrt` function. The three lines are stacked vertically, with the second line's blue box extending further to the right than the first and third lines, suggesting a nested or repeated structure.

So here is a cleaner way of capturing the pattern:

```
(define square (lambda (x) (* x x)))  
(define pythagoras  
  (lambda (x y)  
    (sqrt (+ (square x) (square y))))))
```

Why?

- Breaking computation into modules that capture commonality
 - Enables reuse in other places (e.g. square)
- Isolates (abstracts away) details of computation within a procedure from use of the procedure
 - Useful even if used only *once* (i.e., a unique pattern)

```
(define (comp x y) (/ (+ (* x y) 17) (+ (+ x y) 4)))
```

```
(define (comp x y) (/ (prod+17 x y) (sum+4 x y)))
```

Why?

- May be many ways to divide up

```
(define square (lambda (x) (* x x)))  
(define pythagoras  
  (lambda (x y)  
    (sqrt (+ (square x) (square y))))))
```

```
(define square (lambda (x) (* x x)))  
(define sum-squares  
  (lambda (x y) (+ (square x) (square y))))  
(define pythagoras  
  (lambda (y x) (sqrt (sum-squares y x))))
```

Abstracting the process

- Stages in capturing common patterns of computation
 - Identify modules or stages of process
 - Capture each module within a procedural abstraction
 - Construct a procedure to control the interactions between the modules
 - Repeat the process within each module as necessary

A more complex example

- Remember our method for finding sqrts
 - To find the square root of X
 - Make a guess, called G
 - If G is close enough, stop
 - Else make a new guess by averaging G and X/G

The stages of “SQRT”

- When is something “close enough”
- How do we create a new guess
- How do we control the process of using the new guess in place of the old one

Procedural abstractions

For “close enough”:

```
(define close-enuf?
```

```
  (lambda (guess x)
```

```
    (< (abs (- (square guess) x)) 0.001)))
```



**Note use of procedural
abstraction!**

Procedural abstractions

For “improve”:

```
(define average
```

```
  (lambda (a b) (/ (+ a b) 2)))
```

```
(define improve
```

```
  (lambda (guess x)
```

```
    (average guess (/ x guess))))
```

Why this modularity?

- “Average” is something we are likely to want in other computations, so only need to create once
- Abstraction lets us separate implementation details from use

- Originally:

```
(define average  
  (lambda (a b) (/ (+ a b) 2)))
```

- Could redefine as

```
(define average  
  (lambda (x y) (* (+ x y) 0.5)))
```

- No other changes needed to procedures that use **average**
- Also note that variables (or parameters) are internal to procedure – cannot be referred to by name outside of scope of lambda

Controlling the process

- Basic idea:
 - Given X, G , want **(improve G X)** as new guess
 - Need to make a decision – for this need a new *special form*

(if <predicate> <consequence> <alternative>)

The IF special form

(if <predicate> <consequence> <alternative>)

- Evaluator first evaluates the <predicate> expression.
- If it evaluates to a TRUE value, then the evaluator evaluates and returns the value of the <consequence> expression.
- Otherwise, it evaluates and returns the value of the <alternative> expression.
- **Why must this be a special form? (i.e. why not just a regular lambda procedure?)**

Controlling the process

- Basic idea:

- Given X, G, want **(improve G X)** as new guess
- Need to make a decision – for this need a new *special form*
(if <predicate> <consequence> <alternative>)
- So heart of process should be:

```
(if (close-enuf? G X)
```

```
  G
```

```
    (improve G X) )
```

- But somehow we want to use the value returned by “improving” things as the new guess, and repeat the process

Controlling the process

- Basic idea:
 - Given X, G, want `(improve G X)` as new guess
 - Need to make a decision – for this need a new *special form*
`(if <predicate> <consequence> <alternative>)`
 - So heart of process should be:

```
(define sqrt-loop (lambda (G X)
  (if (close-enuf? G X)
      G
      (sqrt-loop (improve G X) X)
  )
)
```
 - But somehow we want to use the value returned by “improving” things as the new guess, and repeat the process
 - Call process `sqrt-loop` and reuse it!

Putting it together

- Then we can create our procedure, by simply starting with some initial guess:

```
(define sqrt  
  (lambda (x)  
    (sqrt-loop 1.0 x)))
```

Checking that it does the “right thing”

- Next lecture, we will see a formal way of tracing evolution of evaluation process
- For now, just walk through basic steps
 - `(sqrt 2)`
 - `(sqrt-loop 1.0 2)`
 - `(if (close-enuf? 1.0 2))`
 - `(sqrt-loop (improve 1.0 2) 2)`
 - This is just like a normal combination**
 - `(sqrt-loop 1.5 2)`
 - `(if (close-enuf? 1.5 2))`
 - `(sqrt-loop 1.4166666 2)`
- And so on...

Abstracting the process

- Stages in capturing common patterns of computation
 - Identify modules or stages of process
 - Capture each module within a procedural abstraction
 - Construct a procedure to control the interactions between the modules
 - Repeat the process within each module as necessary

Summarizing Scheme

- Primitives

- Numbers **1, -2.5, 3.67e25**
- Strings
- Booleans
- Built in procedures ***, +, -, /, =, >, <**,

-- Names

Creates a loop in system
– allows abstraction of
name for object

- Means of Combination

- (procedure argument₁ argument₂ ... argument_n)

- Means of Abstraction

- Lambda . **Create a procedure**
- Define . **Create names**

- Other forms

- if . **Control order of evaluation**

